Finance Constraint and Firm Investment: 
A Survey of Econometric Methodology

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Received: March 17, 2014              Accepted: April 17, 2014            Online Published: April 28, 2014

doi:10.5430/afr.v3n2p138               URL: http://dx.doi.org/10.5430/afr.v3n2p138

Abstract

It is well established in the macro-finance literature that finance is a crucial factor in the growth process via capital formation, hence the importance of finance constraint in the theory of investment. The issue is particularly important in the emerging market economies which are considered as southern engines of global growth. A very large empirical literature has emerged to test the hypothesis of finance constrained investment since the publication of the seminal paper of Fazzari, Hubbard and Petersen in 1988. The present paper is a survey of the literature. The paper in particular covers the studies on India which as one of the emerging market economies has recently attained its crucial importance for global growth. The paper also provides new research methodology to fill the lacunae in the existing literature.

Keywords: Credit market imperfection, Asymmetric information, Endogenous sample selection, Firm investment in India

JEL Classification: C51; G31; G32; L21

1. Introduction

Economic theory predicts high informational cost in an imperfect capital market because of the presence of asymmetric information between borrowers and lenders. The resultant adverse selection and moral hazard problems affect the efficient operation of the financial market. Consequently firms have to incur higher cost of finance and often a situation may arise where firm investment is constrained by the availability of finance. The issue has been discussed by Stiglitz and Weiss (1981) for the bank credit while Myers and Majluf (1984) has discussed it in the context of equity market. After the financial crisis of 2007 hit the globe the importance of finance constraint has become even more important, because of bank failures, restructuring, new prudential regulations etc. have lead to general non-availability of finance. This has its negative impact on investment, growth and profitability and finally on the stock market. In this backdrop the issue of empirical research on the availability of finance and firm level investment deserves its importance.

The issue is intimately linked with monetary and credit policy in a broader macroeconomic perspective. Bernanke and Gertler (1986) integrates it in a dynamic macroeconomic model to show that financial factors operating at the firm level in the form of insolvency and bankruptcy is capable of initiating and propagating the downturn of a business cycle. The financial crisis of recent vintage, such as 2007 or the earlier one such as the Great Depression of 1930s can be explained in this kind of structure. Gertler (1988) has also argued that the financial factors contributed via the credit squeeze of the banking system in the ‘extra ordinary’ events of 1930s. (Note 1) It is further argued that when firms are finance constrained, the transmission mechanism operating via the interest rate channel does not work resulting into ineffectiveness of the conventional monetary or credit policy. Similar implications are also drawn from Stiglitz and Weiss (1981).

The empirical literature on firm investment in imperfect capital market is substantial though the issue has never died down. Fazzari, Hubbard and Petersen (1988) is the first paper in this area. Later important works include Bond and Meghir (1994), Denis and Sibilkov (2010), Hoshi et al (1991), Kadapakkam et al (1998) etc. A very good survey can be found in Hubbard (1998) and more recent references are also available in Bhaumik, Das and Kumbhakar (2012).

In recent times with the onset of financial sector reforms in many emerging market economies a number of studies have also employed the methodology to investigate the issue as to whether finance constraint has become less severe in the post financial reform period and consequently been able to mitigate lower investment arising out of high cost of finance. This includes Harris, Schiantarelli and Siregar (1994) for Indonesia, Guncavdi, Bleaney and McKay (1998) for Turkey, Gelos and Werner (2002) for Mexico, Wang (2003) for Taiwan, and Koo and Maeng (2005) for South Korea, Bhaduri (2005) and Ghosh (2006) for India. In general it has been found that financial liberalization has led to
reduction in the cost of finance. However, this has not been the outcome always. Gelos and Warner (2002) and Wang (2003) found that small firms have benefited more than their larger counterparts. On the other hand Bhaduri (2005) found that small and new firms in India have been adversely affected by the availability of finance during the post reform period. Such differential impact of financial reform on the availability of finance might be due to country specific factors or other policy measures implemented simultaneously that have interacted with financial market parameters. With this introduction the paper proceeds to Section 2 which considers alternative approaches in modelling econometric equations and major results and finally Section 3 concludes.

2. Econometric Models – Alternative Approaches

The econometric specification of the investment function is derived from firms’ value maximization problem. There are two principal approaches in the empirical literature to tackle the problem of finance constraint. The most popular and widely used is the reduced form regression. It employs Tobin’s Q (Tobin, 1969), defined as the stock market valuation of firms vis-à-vis its replacement cost (capital stock at historical prices adjusted for inflation and depreciation). The other approach is structural model estimation, using the Euler equation. There are also some modified versions of the reduced form approach.

The investment decision of a typical firm $i$ at time $t$ is defined as the solution to the dynamic optimization problem:

$$
\max_{I_t} \left\{ \sum_{s=t}^{\infty} \beta^s \left[ \Pi(K_{is}, \theta_{is}) - C(I_{is}, K_{is}, \lambda_{is}) - p_s I_s \right] \right\}
$$

subject to the capital accumulation constraint $K_t = (1-\delta) K_{t-1} + I_t$, where $\beta = $ subjective discount factor, $\Pi(\cdot) =$ profit function net of taxes, $\theta_i =$ exogenous shock to the profit function, $C(\cdot) =$ adjustment cost function, $p_s =$ tax adjusted relative price of capital goods, $\lambda_s =$ exogenous shock to $C$, $\delta =$ depreciation rate.

The first order condition gives

$$
p_t + C(.) = q_{it}
$$

where

$$
q_{it} = E_t [\sum_{s=t}^{\infty} \beta^s (1-\delta)[\Pi_K - C_K]]
$$

The right hand side on (1) is just the marginal Q which is a sufficient statistic in the absence of capital market imperfection (Hayashi, 1982, Yoshikawa, 1980). Specifying a linear homogeneous $C$ function yields an investment specification (Note 2)

$$
(I_{it} / K_{i,t-1}) = a_i + b \left[q_{it} - p_t \right] + \epsilon_{it}
$$

where $b$ is a parameter of the $C$ function and $\epsilon$ is an optimization error. Under certain assumptions (perfect competition in product and factor markets, homogeneity of fixed capital, linear homogeneity of production and adjustment cost functions, independence of financing and investment decisions) average $Q$, defined as the stock market valuation of firm vis-à-vis its replacement cost, coincides with marginal $Q$. Then the estimable equation becomes

$$
(I_{it} / K_{i,t-1}) = a_i + b \left[Q_{it} + \theta_i \right] + \epsilon_{it}
$$

where $Q_{it}$ is the tax adjusted value of Tobin's $Q$. In more recent studies other variables are also included, such as sales (to capture demand effect) etc. and these variables are generally denoted by vector $X_{it}$. This is a panel data estimation and $a_i$ stands for the firm specific effect for the $i^{th}$ firm.

This form of the investment function holds when there is no friction in the capital market. In the presence of frictions – asymmetric information between lenders and borrowers net worth becomes very important determinant of loan supply to the firm, because net worth determines the collateral strength of the firm. However, there are measurement problems associated with net worth, hence the empirical literature employs cash flow (CF) as the proxy for the change in net worth. Fazzari, Hubbard and Petersen (1988) in their seminal paper proposed the following equation for estimating investment equation of firms likely to face finance constraint

$$
(I_{it} / K_{i,t-1}) = a_i + b \left[Q_{it} + \theta_i \right] + \epsilon_{it}
$$

This approach for estimating investment function is generally followed in the reduced form approach. Later researchers have included balance sheet and other variables, such as market value of debt to total assets, leverage ratio, coverage ratio etc. to capture the impact of financial market imperfections generally denoted by the vector $Z_{it}$. The sample firms are classified into groups of high and low cost of information on the basis of some criterion in the off-sample year(s). Fazzari, Hubbard and Petersen (1988) used dividend pay-out ratio as the criterion. The justification stems from the fact that for a firm, if finance constrained paying high dividends is not consistent with value maximization. Later researchers have used
size, age, credit rating, leverage ratio, main bank system as in Germany or Japan, business group affiliation etc. to classify firms into groups of high information cost and low information cost. Firms in the high cost group are likely to face a finance constraint and vice versa. A positive significant c for high cost firms in the light of the above discussion implies the rejection of the null hypothesis of no finance constraint.

The empirical evidence for the developed countries including the findings of Fazzari et al (1988) is found to be consistent with the predictions of the theory. i.e. firms if found to be finance constrained then the constraint is more biding for group of high information cost than for low information cost whether classified by dividend-payout ratio or size or any other criteria. However, the evidence is not compelling for developing or emerging market economies. Ganesh-Kumar, Sen and Vaidya (2001) found that for the reform period firms with higher export intensity were less constrained in India. Lensink, Van der Molen, and Gangopadhyay (2003) classified firms on the basis of industry group affiliation and found that firms with group affiliation has much lower investment- cash flow sensitivity while George, Kabir and Qian (2010) found no differential sensitivity. (Note 3)

It has been pointed out immediately after the publication of Fazzari et al (1988) that a positive c may result from a number of reasons other than binding finance. For example, a positive demand shock leads to a higher cash flow and consequently higher investment if the demand shock is expected to be permanent (see Kaplan and Zingales, 2000, Laeven, 2003). Fazzari and Petersen (1993) aimed to address this line of criticism and runs as follows. The adjustment cost for working capital investment is lower than for fixed capital, so when a firm’s investment in fixed capital is constrained by the availability of finance the firm reduces investment in working capital. So it is suggested employing the following simultaneous equation system where (4) is substituted by (4) and (5) is another equation for investment in working capital.

\[
\frac{(I_a)}{(K_{it-1})} = a + b \frac{Q_a}{(K_{it-1})} + c \left( \frac{C_{it}}{K_{it-1}} \right) + d \left( \frac{\Delta W_{it}}{K_{it-1}} \right) + \theta_t + \epsilon_{it} \quad (4)
\]

\[
\frac{(\Delta W_{it})}{(K_{it-1})} = e_t + f_{it} + g \left( \frac{C_{it}}{K_{it-1}} \right) + h \left( \frac{W_{it}}{K_{it-1}} \right) + \theta_t + \xi_t \quad (5)
\]

where \( \Delta W_{it} \) = investment in working capital. The firms are classified into groups of differential information cost and estimated using panel data method. A positive (and significant) c together with a negative d implies the presence of finance constraint while a positive d implies increased investment in working capital from a positive demand shock. Fazzari and Petersen (1993) cast some doubt about the findings of Fazzari, Hubbard and Petersen (1988). Bagchi et al (2002) for Indian firms and Ding et al (2013) for Chinese firms are two important examples in this line of research. It may be of interest to know that Bagchi et al (2002) classified firms by dividend pay-out ratio and found that the group of firms with medium dividend pay-out ratio is in fact finance constrained while low dividend paying firms were not. In Germany, as shown by Audretsch and Elston (2002) medium sized firms are most credit constrained which is ascribed to policy of financial infrastructure support to small firms. But in the United States and the United Kingdom, in keeping with the prediction, the smaller firms are more credit constrained.

The reduced form regression though very popular in the literature suffers from the fact that equation (4) or (4') and (5) are employed on the basis of ad hoc reasoning, not derived from well specified objective function. Whited (1992) is the first attempt to derive the investment equation from firms’ value maximization problem with an explicit constraint on the availability of loans and hence called structural equation approach. The objective function is specified as a discounted sum of future dividends which is maximized by choice of investment (or capital stock with appropriate substitution) subject to a non-negativity constraint on the dividends:

\[
d_{it} \geq 0 \quad (6)
\]

This has the same effect as restriction on new share issues, because small increments in outside equity finance also have the same effect on the current stockholders. This is needed for the borrowing constraint to be effective. (Note 4)

The borrowing constraint is introduced in the model by (7) below where the constraint is exogenously given.

\[
B_{it} \leq B_t \quad (7)
\]

The maximization of the value function subject to capital accumulation constraint, (6) and (7) gives two equations. One is the usual first order condition which is some variation of (1) and the combined effects of the two constraints (8) as in below:

\[
(1 + \varphi_{it}) - \beta((1 + r) - \eta_t)E_t(1 + \varphi_{it+1}) - \gamma_t = 0 \quad (8)
\]

where \( \varphi_{it} \) = Lagrange multiplier for (6), \( r_t \) = nominal interest rate on loans net of taxes, \( \eta_t \) = expected rate of inflation and \( \gamma_t \) = Lagrange multiplier for (7). When borrowing constraint does not bind \( \gamma_t \) =0. Substituting for \( \varphi_{it} \) from (8) in (1) one gets the expression for the investment equation to be estimated.
where \( \Phi_h = 1/(1 + \Phi_{h+1}) \), which takes the value zero in the absence of finance constraint. It may be noted that \( \Phi_h \) is also a function of \( \gamma_{it} \) when borrowing constraint binds. For econometric estimation, however there is another problem, viz. that neither of the Lagrange multipliers is observable. So \( \Phi_h \) (and so \( \gamma_{it} \)) is parameterized as function of observed variables that can capture the degree of finance constraint: \( \Phi_h = \Phi(Z_{it}) \). Statistical significance of these variables provides the test of finance constraint. The sample firms are classified into groups of differential cost of information using Moody’s bond rating for the pre-sample period and estimated by dynamic panel method. Introduction of a debt constraint improves the performance of the investment Euler equation for the group of high information cost firms.

All the above methods suffer from the common problem of classification of firms into differential information cost groups on the basis of off sample observations. However, there is no reason why such a classification will remain same over the years. There is another problem, viz. classification criteria based on different variables will in general give different groupings.

To circumvent this problem Hu and Schiantarelli (1998) proposed switching regression approach that takes care of endogenous sample selection. The investment equation is separately specified for high information cost and low information cost firms (in Hu and Schiantarelli terminology high premium and low premium respectively) as given below.

\[
\frac{(I_h^* / K_{h-1}^*)}{Z_{it}^\gamma + u_h < 0} = a_{i1} + X_{it}^{\beta L} + \theta_t + \epsilon_{it} \tag{9}
\]

if

and

\[
\frac{(I_h^* / K_{h-1}^*)}{Z_{it}^\gamma + u_h > 0} = a_{i2} + X_{it}^{\beta H} + \theta_t + \zeta_0 \tag{10}
\]

Two inequalities corresponding to (9) and (10) are called switching functions and used to endogenously selects the \( i^{th} \) firm in \( h^{th} \) year to high or low cost regime. Assuming that the vector of error terms \( (\epsilon_{it}, \zeta_{it}, u_{it}) \sim N(O, \Sigma) \) one can derive the likelihood function:

\[
\log L = \sum_i \sum_t \log (I_{it}) = \sum_i \sum_t \left[ \Phi(Z_{it}) \Phi(-Z_{it}) \right] \frac{1}{2} \sigma_j^2 + \frac{1}{2} \sigma_k^2 + \frac{1}{2} \sigma_u^2 \tag{11}
\]

where \( \sigma_j^2 = \text{var}(j), \sigma_k = \text{cov}(j,k), j,k = e, \zeta, u \).

The log-likelihood function defined as \( L = \sum_i \sum_t \log (I_{it}) \) can be used to estimate \( (\beta^L, \beta^H, \gamma) \). Employing the switching regression method for a set of US firms Hu and Schiantarelli (1998) found that the a very high debt-to-market-value ratio or interest-payments-to-income ratio and low levels of liquidity relative to total capital increase all of which are indicators of financial distress, the probability of incurring higher premium on external finance. Beside of its appeal for handling the issue of exogenous sample splitting bias the method has not been very popular. Bhaduri (2008) employs regime switching approach to a set of Indian firms and reports that cash flow-investment sensitivity is higher for constrained than for unconstrained firms. The probability of finance constraint increases for young, liquidity constrained and low dividend payout firms. In a recent study Gautam and Vaidya (2013) argues that voluntary sale of assets is a cleaner measure of liquidity for finance constrained firms. The paper using switching regression method for a set of Indian firms finds that investment – asset sale sensitivity is higher for finance constrained firms. An important critique of the method is that it treats actual observation as the average of two regimes with the probabilities as the weights. This specification is not entirely correct for each observation also takes a value from the other regime even with a very low weight.

The problem of exogeneity of sample separation of firms into groups of high and low cost of information is taken care of in a recent paper by Bhaumik, Das and Kumbhakar (2012) which draws on stochastic frontier analysis (Kumbhakar and Lovell, 2000). A technical efficient frontier of the investment function is specified and the actual investment is one sided deviation from the efficient frontier. The deviation is modeled in the spirit of imperfect capital market to capture finance constraint. The advantages of this approach are the following. First, sample split into differential information cost group is endogenous. Second, a technical efficiency score for each firm in each period can be calculated which is bounded in \([0, 1]\). This helps find not only the presence of finance constraint but also the degree of severity of the constraint. Finally, it is computationally convenient. (Note 5)
Absent any informational cost the stochastic frontier is specified as some version of (3) 
\[ \ln\left(\frac{I_{it}}{K_{it-1}}\right)^{SF} = \beta X_{it} + \theta_i + a_i + \varepsilon_{it} \]

Denoting the frontier by superscript SF and the deviation by \( u \) the relationship between the frontier and actual investment is given below.

\[ \left(\frac{I_{it}}{K_{it-1}}\right)^{SF} = \left(\frac{I_{it}}{K_{it-1}}\right) \exp(-u_{it}) \Rightarrow \ln\left(\frac{I_{it}}{K_{it-1}}\right) = \ln\left(\frac{I_{it}}{K_{it-1}}\right)^{SF} - u_{it} \]

The higher the value of \( u \) greater is the impact of constraints on investment. If \( u \) is close to zero for some firms then those firms are not supposedly constrained. Specifically, technical efficiency is the investment efficiency defined as the ratio of actual to the efficient investment (i.e., \( \exp(-u) \) which will be bounded between 0 and 1). The efficiency score is estimated for each observation using the frontier technique. Apart from the ease of interpretation, the technical efficiency score has the advantage of capturing the combined impact of all the constraining variables on the extent of credit constraint.

Next the inefficiency because of finance constraint is modelled in terms of firm characteristics, \( Z \) variables. Assuming credit constraint.

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\[ u_{it} - N(0, \sigma^2_{it}(Z_{it})), \ u_{it} \geq 0 \text{ where } \sigma^2(Z_{it}) = \exp(\gamma Z_{it}) \text{ to maintain non-negativity, we have} \]

\[ E(u_{it}) = \sqrt{2/\pi}\sigma(Z_{it}) = \sqrt{2/\pi}\exp(\gamma Z_{it}). \]

Thus one can easily find the marginal effect of the \( Z \) variables on investment inefficiency. Indeed, it can be argued that (variations of) the specification used in the OLS and fixed effects panel approaches are a special case of the stochastic frontier model.

Letting \( v_{it} = e_{it} - u_{it} \), \( E(v_{it}) \neq 0 \) because \( u_{it} \neq 0 \), which poses a problem in using LS method. The problem can be circumvented in the following way. \( v_{it} = e_{it} - u_{it} = e_{it} - [u_{it} - E(u_{it})] = E(u_{it}) = e_{it} - E(u_{it}) \) where \( E(e_{it}) = 0 \) by construction. To account for the extra term - \( E(u_{it}) \), it is assumed that \( -E(u_{it}) = \gamma Z_{it} \). Thus the stochastic formulation of the baseline model:

\[ \ln\left(\frac{I_{it}}{K_{it-1}}\right) = \beta X_{it} + \theta_i + a_i + e_{it} - u_{it} \]

along with

\[ -E(u_{it}) = \gamma Z_{it} \]

completes the econometric specification. One can justify the use of (3) starting from a frontier model. (12) ensures the assumptions on \( u \) and \( v \) so that \(-E(u_{it}) < 0\), and thus one can estimate the extent of credit constraint of a firm in each of the years of analysis.

Bhaumik et al (2012) applied the technique for around 600 Indian firms for the period 1996-97 to 2005-06. The paper compares different methods of estimation including OLS pooled regression, standard Fazzari, Hubbard, Petersen type panel regression and compares the results with the stochastic frontier formulation. The regression results of the stochastic frontier formulation are consistent with other methods of estimation, but the robustness results differ. In the stochastic frontier formulation the paper includes (log of) sales and lagged sales along with \( Q \) in \( X \) and cash flow, asset, leverage and a dummy for business group affiliation in \( Z \). The best fit for leverage obtains for a dummy defined if debt-equity ratio exceeds 1.8. The estimate regression equation is given below.

\[ \ln\left(\frac{I_{it}}{K_{it-1}}\right)^{SF} = -2.5 + 0.06 \ln Q_{it} + 0.93 \ln\left(\text{SALE}_{it}/K_{it-1}\right) + 0.38 \ln\left(\text{SALE}_{it-1}/K_{it-2}\right) \]

\[ \gamma Z_{it} = 0.58 - 0.10(CF_{it}/K_{it-1}) - 0.07 \ln(\text{ASSET}_{it}) + 0.21 \text{LEVERAGE}_{it} - 0.62 \text{BUNINESSGROUP}_{it} + 0.07 \text{GROUP}^2_{it} \times \text{TIME} \]

All the coefficients are significant at 1% or 5%. The paper also estimates inefficiency for \( Z \) variables in different percentiles. It is found that inefficiency decreases at higher percentiles. Comparison of the distributions of firms between 1996-97 and 2005-06 shows that the distributions of small and large firms (size measured by sales), distributions of high indebted and low indebted firms coincide across the periods. Business group affiliation while alleviates finance constraint confirming its positive role in an imperfect capital market, but the effect dissipates with time. The latter indicates the opaque structure of business group affiliation and questionable corporate governance qualities outweighs the benefits associated with them in an imperfect capital market as reforms progress. (Note 6) This clearly shows that economic reforms initiated in 1990s have some impact on the Indian capital market.

3. Conclusion

This paper provides a survey of the different strands of empirical methods for estimating firm investment in an imperfect capital market. The paper elucidates the relative merits and demerits of the different methods. The literature has never been dead for two reasons, viz. the issue is very much live and secondly there exists many a lacunae which
gives the scope of new studies. The econometric models so far analyzed can also be extended to include the stock price performance of firms with their status of finance constraint as the deviation from the optimal investment frontier. The empirical observations of the finance constrained firms are very useful in drawing up monetary and credit policy in an economy.

Acknowledgements

An earlier version of the paper was presented at the World Statistics Conference 2013 held in Hong Kong. The author is indebted to Amiya Kumar Bagchi, Sumon Bhaumik, Subal Kumbhakar, Sugata Marjit for helpful comments and suggestions on several occasions. The author is also grateful to Gopal K. Basak and Ngai Hang Chan, the organizers of the session on Finance and contemporary issues (ST073) of the World Statistics Congress 2013 for invitation and a number of participants in the conference who had commented on the paper. The usual disclaimer applies.

References


**Notes**

Note 1. Friedman and Schwartz (1963) based on rigorous empirical work argues that the Great Depression is the result of series of bank failures. This view is contrary to Keynesian revolution.

Note 2. \[ C(I_1, K_1) = \frac{a}{2} (I_1 / K_1 - \alpha_1 - \lambda_1)^2 K_1 \].

Note 3. Athley, and Laumas (1994) using a somewhat different approach found that internal funds are more important for firm investment, the sensitivity is higher for larger and firms producing luxury goods.

Note 4. Whited (1992) argues on the basis of empirical facts that firms are dependent on borrowing than new share issue for raising finance.

Note 5. Wang (2003) is an earlier contribution along this line.